# First Photometric Analysis of the Solar-Type Binary, V428 Cep (NSV 395), in the field of NGC 188 

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#### Abstract

V428 Cep (or NSV 395) is a faint 15th magnitude binary observed in a study of the open cluster NGC 188. However, its distance from the core of the cluster might exclude its membership. Its light curve was classified as a short period EB type eclipsing binary with a period of 0.3079 d and an amplitude of $\sim 0.7$ magnitude in all curves. The difference in component temperatures is some $\Delta \mathrm{T}=180 \mathrm{~K}$ and its fill-out is a hefty $35 \%$. A brief, 2.5 year period study yields, as expected, a constant period, which is 0.3076789 d . More monitoring is needed to determine its true orbital evolution. The inclination, $80^{\circ}$ is not quite enough to produce total eclipses, so a q-search was performed using the September 17, 2004 version of the Wilson-Devinney program. Our lowest residual solution gives a $\mathrm{q}=0.4$. A cool spot was modeled on the primary component to take care of the light curve asymmetries. V428 Cep is a K-type W UMa contact binary.


## 1. Introduction

This paper represents the first precision, four-color, BVRI photometric study of this interesting contact binary which is in the field of the open cluster NGC 188.

## 2. History and observations

The variable was originally listed as short period variable NSV 395 (S8282) from photographic data (Hoffmeister 1964). It was observed in a study of the very old open cluster (age 5-7 Gyr) NGC 188 (Popov et al. 2013). This cluster age is what we might expect for such a W UMa binary. This paper designated it as a $\beta$ Lyr-type eclipsing binary with a period of 0.3077 day and an Rmag range of 14.392-15.675 and a secondary minimum of 15.552 . They gave the first published ephemeris:

$$
\begin{equation*}
\mathrm{JD} \text { Hel MinI }=2455632.260+0.3077 \mathrm{~d} \times \mathrm{E} . \tag{1}
\end{equation*}
$$

Popov et al.'s (2013) CCD light curves are given in Figure 1.
This system was observed as a part of our student/ professional collaborative studies of interacting binaries from data taken from Dark Sky Observatory (DSO) observations. The observations were taken by Dr. Dan Caton, Dr. Ron Samec, and Jeremy Clark. Reduction and analyses were mostly done by Dr. Samec and David Maloney. Our 2013 BVRI light curves
were taken with the DSO 0.81-meter reflector at Philips Gap, North Carolina, on 2, 3, and 4 November 2013 with a thermoelectrically cooled $\left(-40^{\circ} \mathrm{C}\right) 2 \mathrm{KX} 2 \mathrm{~K}$ Apogee Alta camera.

Individual observations included 128 in B and R , and 132 in V and I . The probable error of a single observation was $2 \%$ in B and V , and $1 \%$ in R and I . The relatively large errors are assumed due to the faintness of the binary. Figures $2 a$ and $2 b$ show sample observations of R, I, and R-I color curves on the night of 2 November, and of B, V, and B-V color curves on the night of 3 November 2013, respectively.

Our complete observations are given in Table 1, in delta magnitudes, $\Delta \mathrm{B}, \Delta \mathrm{V}, \Delta \mathrm{R}_{\mathrm{c}}$ and $\Delta \mathrm{I}_{\mathrm{c}}$, in the sense of variable minus comparison star (V-C), phased with Equation 2.

## 3. Finding chart

The finding chart, given here for future observers, is shown in Figure 3. The coordinates and magnitudes of the variable star, comparison star, and check star are given in Table 2. The $\mathrm{C}-\mathrm{K}$ values stayed fairly constant throughout the observing run, varying $1-2 \%$.

## 4. Period study

Five times of minimum light were calculated, three primary and two secondary eclipses from our present observations:


Figure 1. V428 Cep-NGC 188. R, I CCD light curves were taken by Popov et al. 2013.


Figure 2a. V428 Cep-NGC 188. R (middle), I (bottom) delta magnitudes from sample observations and color curve (top) on 2 November 2013.


Figure 2b. V428 Cep-NGC 188. B (middle), V (bottom) delta magnitudes and color curve (top) on 3 November 2013.

$$
\begin{aligned}
\text { HJD I }= & 2456598.6746 \pm 0.0007 \\
& 2456599.5990 \pm 0.0014 \\
& 2456600.8292 \pm 0.0013
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{HJD} \mathrm{II}= & 2456598.8299 \pm 0.0026 \\
& 2456599.7549 \pm 0.00025 .
\end{aligned}
$$

Six CCD times of minimum light were determined using previous observations of Popov et al. 2013. These were included in our determination of an improved linear ephemeris:

$$
\begin{array}{r}
\text { HJD MinI }=2456599.5990+0.30767914 \times \mathrm{E}  \tag{2}\\
\pm 0.0010 \pm 0.00000043
\end{array}
$$

Since this study covers only 2.5 years of observations, at least 10 more years of patrolling are needed to determine if the period is


Figure 3. V428 Cep-NGC 188 finding chart. V428 Cep Variable (V), Comparison (C) and Check (K).
changing. The times of minimum light and the linear residuals are given in Table 3. Figure 4 shows the linear residuals ( $\mathrm{O}-\mathrm{C}$ 's) from this calculation.

## 5. NGC 188

NGC 188 is an old open cluster of age 5-10 Gyr and has quite a few W UMa binaries (for example, six in Zhang et al. 2002), which fall in this age range. From his analysis of the precontact W UMa binary, V12, Meibom (2009) gives a cluster distance of $1,770 \pm 75 \mathrm{pc}$ and a main sequence age of $6.2 \pm 0.2 \mathrm{Gyr}$. The position of V428 Cep on the color magnitude diagram is to the right of the main sequence branch before the turnoff, as expected for this cool-type binary system. We believe that the binary could well be a part of the cluster despite its position in the field ( 43 ' from the cluster center). W UMa binaries are noted for having high velocity dispersions, and it may be escaping the cluster (Guinan and Bradstreet 1988). The R, R-I color magnitude diagram is shown in Figure 5.

## 6. Light curve characteristics

The light curves were phased using Equation (2). These are given in Figures 6a and 6b. A table of light curve characteristics is given in Table 4. The curves are only of fair precision, averaging between 1 and $3 \%$, probably due to the binary's faintness. The amplitude of the light curve varies from 0.76 to 0.65 magnitude in B to I, respectively. The O'Connell effect (the difference in maxima), which is classically an indication of spot activity, is slightly larger than the scatter/ averaging $4 \%$. The difference between the two minima is substantial for a W UMa binary, some 0.1-0.2 magnitude, and is undoubtedly the reason it was designated a $\beta$ Lyr type EB by Popov et al. (2013). However, the light curve characteristics point to a

Table 1. V428 Cep-NGC 188 observations, $\Delta B, \Delta V, \Delta R$, and $\Delta I$, variable star minus comparison star.

| $\Delta B$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ | $\Delta B$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ | $\Delta B$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ | $\Delta B$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ | $\Delta B$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5.486 | 98.5258 | 5.029 | 98.7333 | 5.187 | 99.4821 | 5.024 | 99.6427 | 5.538 | 99.7570 |
| 5.404 | 98.5315 | 4.986 | 98.7417 | 5.075 | 99.4844 | 4.977 | 99.6475 | 5.523 | 99.7618 |
| 5.367 | 98.5372 | 4.947 | 98.7501 | 5.082 | 99.4906 | 5.036 | 99.6516 | 5.372 | 99.7659 |
| 5.236 | 98.548 | 4.957 | 98.7602 | 5.033 | 99.4929 | 4.908 | 99.6565 | 5.241 | 99.7701 |
| 5.055 | 98.5584 | 4.975 | 98.7686 | 4.905 | 99.4951 | 4.957 | 99.6606 | 5.298 | 99.7750 |
| 5.028 | 98.5658 | 5.044 | 98.777 | 4.913 | 99.4974 | 4.861 | 99.6648 | 5.292 | 99.7792 |
| 4.983 | 98.5731 | 5.055 | 98.7854 | 4.915 | 99.5029 | 4.900 | 99.6707 | 5.083 | 99.7833 |
| 4.928 | 98.5804 | 5.156 | 98.7938 | 4.884 | 99.511 | 4.888 | 99.6749 | 5.071 | 99.7876 |
| 4.941 | 98.5878 | 5.252 | 98.8044 | 4.937 | 99.5175 | 4.882 | 99.679 | 5.000 | 99.7917 |
| 4.901 | 98.5968 | 5.378 | 98.8128 | 4.920 | 99.525 | 4.855 | 99.684 | 4.983 | 99.7961 |
| 4.910 | 98.6041 | 5.527 | 98.8212 | 4.906 | 99.5323 | 4.952 | 99.6882 | 5.026 | 100.7737 |
| 4.922 | 98.6115 | 5.524 | 98.8296 | 4.945 | 99.5391 | 4.946 | 99.6924 | 5.011 | 100.7807 |
| 4.996 | 98.6188 | 5.440 | 98.838 | 5.016 | 99.5455 | 4.942 | 99.6965 | 5.050 | 100.7877 |
| 5.040 | 98.6262 | 5.302 | 98.8475 | 4.983 | 99.5519 | 5.000 | 99.7007 | 5.128 | 100.7948 |
| 5.115 | 98.6362 | 5.133 | 98.8559 | 5.043 | 99.5604 | 4.919 | 99.7048 | 5.196 | 100.8026 |
| 5.202 | 98.6436 | 5.025 | 98.8644 | 5.169 | 99.5702 | 5.070 | 99.7097 | 5.351 | 100.8097 |
| 5.279 | 98.6509 | 4.904 | 98.8727 | 5.371 | 99.581 | 5.102 | 99.7139 | 5.516 | 100.8171 |
| 5.335 | 98.6584 | 5.004 | 98.8811 | 5.606 | 99.5923 | 5.126 | 99.718 | 5.615 | 100.8241 |
| 5.518 | 98.6657 | 4.941 | 98.9113 | 5.718 | 99.6043 | 5.086 | 99.7227 | 5.673 | 100.8311 |
| 5.564 | 98.6738 | 4.999 | 98.9221 | 5.540 | 99.6136 | 5.182 | 99.7268 | 5.600 | 100.8382 |
| 5.539 | 98.6822 | 5.019 | 98.9302 | 5.390 | 99.6188 | 5.290 | 99.731 | 5.397 | 100.8456 |
| 5.366 | 98.6906 | 5.115 | 98.941 | 5.274 | 99.6226 | 5.350 | 99.7352 | 5.288 | 100.8534 |
| 5.205 | 98.699 | 5.263 | 98.9519 | 5.319 | 99.6265 | 5.281 | 99.7393 | 5.100 | 100.8608 |
| 5.099 | 98.7074 | 5.655 | 98.9599 | 5.201 | 99.6301 | 5.494 | 99.7435 | 5.018 | 100.8678 |
| 5.001 | 98.7165 | 4.989 | 99.4776 | 5.097 | 99.6339 | 5.588 | 99.7487 |  |  |
| 5.064 | 98.7249 | 5.084 | 99.4799 | 5.171 | 99.6375 | 5.443 | 99.7528 |  |  |
| $\Delta V$ | $H J D$ | $\Delta V$ | $H J D$ | $\Delta V$ | $H J D$ | $\Delta V$ | $H J D$ | $\Delta V$ | $H J D$ |
|  | 2455800+ |  | $2455800+$ |  | $2455800+$ |  | $2455800+$ |  | $2455800+$ |
| 5.227 | 98.524 | 4.702 | 98.7388 | 4.946 | 99.479 | 4.778 | 99.650 | 5.137 | 99.769 |
| 5.173 | 98.530 | 4.679 | 98.7472 | 4.959 | 99.481 | 4.756 | 99.654 | 5.122 | 99.773 |
| 5.071 | 98.535 | 4.661 | 98.7556 | 4.881 | 99.484 | 4.763 | 99.659 | 5.001 | 99.778 |
| 5.009 | 98.541 | 4.696 | 98.7657 | 4.900 | 99.486 | 4.736 | 99.663 | 4.951 | 99.782 |
| 4.841 | 98.553 | 4.727 | 98.7741 | 4.790 | 99.492 | 4.744 | 99.668 | 4.838 | 99.786 |
| 4.790 | 98.563 | 4.764 | 98.7825 | 4.821 | 99.494 | 4.721 | 99.673 | 4.776 | 99.790 |
| 4.734 | 98.571 | 4.838 | 98.7909 | 4.784 | 99.497 | 4.715 | 99.678 | 4.738 | 99.794 |
| 4.684 | 98.578 | 4.912 | 98.7993 | 4.785 | 99.499 | 4.732 | 99.682 | 4.712 | 99.799 |
| 4.677 | 98.585 | 5.029 | 98.8099 | 4.710 | 99.509 | 4.740 | 99.687 | 4.708 | 100.759 |
| 4.653 | 98.593 | 5.149 | 98.8183 | 4.743 | 99.514 | 4.756 | 99.691 | 4.690 | 100.768 |
| 4.653 | 98.602 | 5.300 | 98.8267 | 4.677 | 99.522 | 4.757 | 99.695 | 4.713 | 100.778 |
| 4.674 | 98.609 | 5.270 | 98.8351 | 4.697 | 99.530 | 4.764 | 99.699 | 4.749 | 100.785 |
| 4.702 | 98.616 | 5.103 | 98.8435 | 4.690 | 99.536 | 4.784 | 99.703 | 4.826 | 100.792 |
| 4.760 | 98.624 | 4.972 | 98.853 | 4.701 | 99.543 | 4.738 | 99.708 | 4.906 | 100.799 |
| 4.759 | 98.631 | 4.864 | 98.8615 | 4.729 | 99.550 | 4.805 | 99.712 | 5.042 | 100.807 |
| 4.883 | 98.641 | 4.815 | 98.8698 | 4.760 | 99.556 | 4.833 | 99.717 | 5.177 | 100.814 |
| 4.951 | 98.649 | 4.780 | 98.8782 | 4.927 | 99.565 | 4.864 | 99.721 | 5.337 | 100.821 |
| 5.093 | 98.656 | 4.732 | 98.8866 | 5.172 | 99.576 | 4.924 | 99.725 | 5.362 | 100.828 |
| 5.247 | 98.663 | 4.683 | 98.8953 | 5.364 | 99.587 | 4.928 | 99.730 | 5.355 | 100.835 |
| 5.344 | 98.671 | 4.675 | 98.9019 | 5.357 | 99.616 | 5.000 | 99.734 | 5.199 | 100.843 |
| 5.360 | 98.679 | 4.677 | 98.9069 | 5.208 | 99.621 | 5.039 | 99.738 | 5.043 | 100.850 |
| 5.206 | 98.688 | 4.696 | 98.9164 | 5.124 | 99.625 | 5.121 | 99.742 | 4.894 | 100.858 |
| 5.028 | 98.696 | 4.749 | 98.9272 | 5.033 | 99.629 | 5.206 | 99.746 | 4.784 | 100.865 |
| 4.902 | 98.705 | 4.766 | 98.9353 | 4.912 | 99.632 | 5.275 | 99.751 | 4.752 | 100.872 |
| 4.813 | 98.713 | 4.859 | 98.9462 | 4.853 | 99.636 | 5.283 | 99.756 |  |  |
| 4.739 | 98.722 | 5.062 | 98.957 | 4.867 | 99.640 | 5.248 | 99.760 |  |  |
| 4.740 | 98.7304 | 5.087 | 98.965 | 4.778 | 99.645 | 5.214 | 99.765 |  |  |

Table 1. V428 Cep-NGC 188 observations, $\Delta \mathrm{B}, \Delta \mathrm{V}, \Delta \mathrm{R}$, and $\Delta \mathrm{I}$, variable star minus comparison star, cont.

| $\Delta R$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ | $\Delta R$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ | $\Delta R$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ | $\Delta R$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ | $\Delta R$ | $\begin{gathered} H J D \\ 2455800+ \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4.933 | 98.523 | 4.425 | 98.745 | 4.544 | 99.481 | 4.502 | 99.644 | 4.817 | 99.763 |
| 4.918 | 98.528 | 4.385 | 98.754 | 4.512 | 99.483 | 4.453 | 99.649 | 4.814 | 99.767 |
| 4.574 | 98.551 | 4.414 | 98.764 | 4.504 | 99.485 | 4.441 | 99.653 | 4.738 | 99.772 |
| 4.513 | 98.562 | 4.455 | 98.772 | 4.477 | 99.492 | 4.392 | 99.658 | 4.639 | 99.777 |
| 4.475 | 98.569 | 4.490 | 98.781 | 4.471 | 99.494 | 4.418 | 99.662 | 4.631 | 99.781 |
| 4.429 | 98.577 | 4.562 | 98.789 | 4.447 | 99.496 | 4.389 | 99.666 | 4.614 | 99.785 |
| 4.415 | 98.584 | 4.723 | 98.808 | 4.467 | 99.498 | 4.367 | 99.672 | 4.542 | 99.789 |
| 4.406 | 98.591 | 4.843 | 98.816 | 4.417 | 99.507 | 4.379 | 99.676 | 4.514 | 99.793 |
| 4.413 | 98.600 | 4.979 | 98.825 | 4.399 | 99.513 | 4.383 | 99.681 | 4.518 | 99.798 |
| 4.401 | 98.608 | 5.004 | 98.833 | 4.409 | 99.520 | 4.397 | 99.686 | 4.389 | 100.759 |
| 4.438 | 98.615 | 4.868 | 98.842 | 4.415 | 99.528 | 4.396 | 99.690 | 4.399 | 100.767 |
| 4.467 | 98.622 | 4.765 | 98.851 | 4.402 | 99.535 | 4.429 | 99.698 | 4.449 | 100.777 |
| 4.510 | 98.630 | 4.658 | 98.860 | 4.442 | 99.542 | 4.472 | 99.702 | 4.475 | 100.784 |
| 4.550 | 98.640 | 4.548 | 98.868 | 4.484 | 99.548 | 4.502 | 99.706 | 4.552 | 100.791 |
| 4.662 | 98.647 | 4.517 | 98.876 | 4.505 | 99.555 | 4.490 | 99.711 | 4.622 | 100.798 |
| 4.791 | 98.654 | 4.464 | 98.885 | 4.580 | 99.564 | 4.528 | 99.715 | 4.752 | 100.806 |
| 4.935 | 98.662 | 4.406 | 98.892 | 4.720 | 99.574 | 4.585 | 99.720 | 4.879 | 100.813 |
| 5.061 | 98.669 | 4.394 | 98.900 | 4.945 | 99.585 | 4.612 | 99.724 | 5.055 | 100.820 |
| 5.097 | 98.677 | 4.410 | 98.905 | 4.950 | 99.605 | 4.685 | 99.728 | 5.081 | 100.827 |
| 4.985 | 98.686 | 4.430 | 98.915 | 4.867 | 99.615 | 4.738 | 99.733 | 5.045 | 100.834 |
| 4.795 | 98.694 | 4.440 | 98.925 | 4.774 | 99.620 | 4.804 | 99.737 | 4.820 | 100.841 |
| 4.657 | 98.703 | 4.496 | 98.933 | 4.688 | 99.624 | 4.835 | 99.741 | 4.774 | 100.849 |
| 4.578 | 98.711 | 4.557 | 98.944 | 4.644 | 99.628 | 4.951 | 99.745 | 4.670 | 100.856 |
| 4.505 | 98.720 | 4.697 | 98.955 | 4.557 | 99.632 | 4.966 | 99.750 | 4.560 | 100.864 |
| 4.453 | 98.729 | 4.809 | 98.963 | 4.561 | 99.635 | 4.990 | 99.754 |  |  |
| 4.436 | 98.737 | 4.535 | 99.479 | 4.520 | 99.639 | 4.930 | 99.759 |  |  |
| $\Delta I$ | HJD | $\Delta I$ | HJD | $\Delta I$ | HJD | $\Delta I$ | HJD | $\Delta I$ | HJD |
|  | 2455800+ |  | 2455800+ |  | 2455800+ |  | 2455800+ |  | 2455800+ |
| 4.642 | 98.522 | 4.702 | 98.739 | 4.946 | 99.479 | 4.778 | 99.650 | 5.137 | 99.769 |
| 4.648 | 98.527 | 4.679 | 98.747 | 4.959 | 99.481 | 4.756 | 99.654 | 5.122 | 99.773 |
| 4.590 | 98.533 | 4.661 | 98.756 | 4.881 | 99.484 | 4.763 | 99.659 | 5.001 | 99.778 |
| 4.496 | 98.539 | 4.696 | 98.766 | 4.900 | 99.486 | 4.736 | 99.663 | 4.951 | 99.782 |
| 4.343 | 98.550 | 4.727 | 98.774 | 4.790 | 99.492 | 4.744 | 99.668 | 4.838 | 99.786 |
| 4.243 | 98.561 | 4.764 | 98.783 | 4.821 | 99.494 | 4.721 | 99.673 | 4.776 | 99.790 |
| 4.203 | 98.568 | 4.838 | 98.791 | 4.784 | 99.497 | 4.715 | 99.678 | 4.738 | 99.794 |
| 4.163 | 98.575 | 4.912 | 98.799 | 4.785 | 99.499 | 4.732 | 99.682 | 4.712 | 99.799 |
| 4.163 | 98.583 | 5.029 | 98.810 | 4.710 | 99.509 | 4.740 | 99.687 | 4.708 | 100.759 |
| 4.142 | 98.590 | 5.149 | 98.818 | 4.743 | 99.514 | 4.756 | 99.691 | 4.690 | 100.768 |
| 4.143 | 98.599 | 5.300 | 98.827 | 4.677 | 99.522 | 4.757 | 99.695 | 4.713 | 100.778 |
| 4.136 | 98.606 | 5.270 | 98.835 | 4.697 | 99.530 | 4.764 | 99.699 | 4.749 | 100.785 |
| 4.155 | 98.614 | 5.103 | 98.844 | 4.690 | 99.536 | 4.784 | 99.703 | 4.826 | 100.792 |
| 4.211 | 98.621 | 4.972 | 98.853 | 4.701 | 99.543 | 4.738 | 99.708 | 4.906 | 100.799 |
| 4.234 | 98.628 | 4.864 | 98.862 | 4.729 | 99.550 | 4.805 | 99.712 | 5.042 | 100.807 |
| 4.308 | 98.638 | 4.815 | 98.870 | 4.760 | 99.556 | 4.833 | 99.717 | 5.177 | 100.814 |
| 4.394 | 98.646 | 4.780 | 98.878 | 4.927 | 99.565 | 4.864 | 99.721 | 5.337 | 100.821 |
| 4.496 | 98.653 | 4.732 | 98.887 | 5.172 | 99.576 | 4.924 | 99.725 | 5.362 | 100.828 |
| 4.633 | 98.661 | 4.683 | 98.895 | 5.364 | 99.587 | 4.928 | 99.730 | 5.355 | 100.835 |
| 4.786 | 98.668 | 4.675 | 98.902 | 5.357 | 99.616 | 5.000 | 99.734 | 5.199 | 100.843 |
| 4.816 | 98.676 | 4.677 | 98.907 | 5.208 | 99.621 | 5.039 | 99.738 | 5.043 | 100.850 |
| 4.776 | 98.685 | 4.696 | 98.916 | 5.124 | 99.625 | 5.121 | 99.742 | 4.894 | 100.858 |
| 4.574 | 98.693 | 4.749 | 98.927 | 5.033 | 99.629 | 5.206 | 99.746 | 4.784 | 100.865 |
| 4.418 | 98.701 | 4.766 | 98.935 | 4.912 | 99.632 | 5.275 | 99.751 | 4.752 | 100.872 |
| 4.314 | 98.710 | 4.859 | 98.946 | 4.853 | 99.636 | 5.283 | 99.756 |  |  |
| 4.242 | 98.719 | 5.062 | 98.957 | 4.867 | 99.640 | 5.248 | 99.760 |  |  |
| 4.199 | 98.727 | 5.087 | 98.965 | 4.778 | 99.645 | 5.214 | 99.765 |  |  |

Table 2. Information on the stars used in this study.

| Star | Name | $\begin{aligned} & \text { R.A. (2000) } \\ & h m \quad s \end{aligned}$ | $\begin{gathered} \text { Dec. (2000) } \\ \circ \end{gathered}$ | V | $B-V$ | $J-K$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V | 3UC350-001392 ${ }^{1}$ | 010812.900 | +843806.00 | 15.51 | - | 0.581 |
| C | TYC 4619738 | 010754.577 | +843330.58 ${ }^{2}$ | 10.917 | 0.535 |  |
| K (Check) | TYC 4619618 | 010729.1344 | +844041.871 ${ }^{2}$ | 12.029 | 0.813 |  |

${ }^{1}$ USNO CCD Astrograph Catalog (Zacharias et al. 2012). ${ }^{2}$ TYCHO (Perryman et al. 1997).

Table 3. V428 Cep-NGC 188 times of minimum light and linear residuals.

| No. | Epoch <br> HJD 2400000+ | Cycle | Weight | $O-C$ | Reference |
| ---: | ---: | ---: | ---: | ---: | :--- |
| 1 | 55632.2584 | -3144.0 | 1.0 | 0.0026 | Popov et al. 2012 |
| 2 | 55635.3352 | -3134.0 | 1.0 | 0.0026 | Popov et al. 2012 |
| 3 | 55638.2565 | -3124.5 | 0.5 | 0.0009 | Popov et al. 2012 |
| 4 | 55638.2593 | -3124.5 | 0.5 | 0.0037 | Popov et al. 2012 |
| 5 | 55639.3325 | -3121.0 | 1.0 | 0.0000 | Popov et al. 2012 |
| 6 | 55640.2480 | -3118.0 | 1.0 | -0.0075 | Popov et al. 2012 |
| 7 | 56598.6746 | -3.0 | 1.0 | -0.0014 | Present Observations |
| 8 | 56598.8299 | -2.5 | 1.0 | 0.0001 | Present Observations |
| 9 | 56599.5990 | 0.0 | 1.0 | 0.0000 | Present Observations |
| 10 | 56599.7549 | 0.5 | 1.0 | 0.0020 | Present Observations |
| 11 | 56600.8292 | 4.0 | 1.0 | -0.0006 | Present Observations |



Figure 4. V428 Cep-NGC 188. Linear O-C residuals from the period study.


Figure 5. V428 Cep-NGC 188. R, R-I color magnitude diagram of NGC 188 with the turnoff and the position of V428 Cep identified.
contact binary-the B-V color curves dip downward at phase 0.0 and at phase 0.5 , which point to each component filling its Roche Lobe. At each quadrature, beginning at phase 0.0 , the $\Delta(\mathrm{B}-\mathrm{V})$ values are $0.31,0.20,0.24$, and 0.23 , respectively. Thus, the curves indicate a contact, classical EW-type binary.

## 7. Temperature

Table 4 of Popov et al. (2013) gives the color indices of the newly discovered variable stars. The V428 Cep spectral type is given as K1. Its period tells us it is of class V. So we have assigned the temperature 5000 K (spectral type, K2V) to the primary component. These results closely match those of 2MASS photometry. Although its faintness is of the right magnitude and its placement is to the right of the main sequence of the CMD (Bettis 1975), its spatial position is rather far from the center of the cluster. It is assumed to be a field star (see section 4). It is of interest that K-type contact binaries, with periods shorter than 0.3 day, and the period of V428 Cep is on the borderline, are important objects for explaining the period cutoff phenomenon (Liu et al. 2014).

## 8. Synthetic light curve solution

The B, V, R, and I curves were pre-modeled with binary mAKER 3.0 (Bradstreet and Steelman 2002) and fits were determined in all filter bands. The resulting parameters were then averaged and input into a four-color simultaneous light curve calculation using the Wilson-Devinney Program (wd; Wilson and Devinney 1971; Wilson 1990, 1994; van Hamme and Wilson 1998). The solution was computed in Mode 3 (contact mode). Convective parameters $\mathrm{g}=0.32$, $\mathrm{A}=0.5$ were used.

Since eclipses did not appear to be quite total, a $q\left(m_{2} / m_{1}\right)$ search was performed over the range $q=0.27$ to 4.0 (see Figure 7). The sum of square residuals minimized at approximately $\mathrm{q}=0.4$. Beginning at this value, q was included with the rest of the adjustable parameters to obtain a final solution. The solution is given in Table 5. The normalized curves overlain by our light curve solutions are shown as Figures 8a and 8 b . The geometrical (Roche-Lobe) representation of the system is given in Figures 9a, b, c, and d at the light curve quadratures so that the reader may see the placement of the spot and the relative size of the stars as compared to the orbit.

## 9. Discussion

V428 Cep in the field of NGC 188 is a W UMa binary in a classic contact configuration. Its spectral type, K1V, indicates

Table 4. V428 Cep-NGC 188 light curve characteristics.

| Filter | Phase | Magnitude Max. I | Phase | Magnitude <br> Max. II |
| :---: | :---: | :---: | :---: | :---: |
|  | 0.25 |  | 0.75 |  |
| B |  | $4.91 \pm 0.04$ |  | $4.92 \pm 0.03$ |
| V |  | $4.71 \pm 0.03$ |  | $4.68 \pm 0.03$ |
| R |  | $4.38 \pm 0.01$ |  | $4.40 \pm 0.01$ |
| I |  | $4.12 \pm 0.01$ |  | $4.17 \pm 0.02$ |
| Filter | Phase | Magnitude <br> Min. II | Phase | Magnitude <br> Min. I |
|  | 0.50 |  | 0.00 |  |
| B |  | $5.51 \pm 0.05$ |  | $5.66 \pm 0.06$ |
| V |  | $5.27 \pm 0.02$ |  | $5.35 \pm 0.01$ |
| R |  | $4.96 \pm 0.03$ |  | $5.07 \pm 0.01$ |
| I |  | $4.67 \pm 0.01$ |  | $4.82 \pm 0.02$ |
| Filter | Min. $I-$ Max. I | Max. IMax. II | Phase | Min. I- <br> Min. II |
| B | 0.76 | $0.10 \pm-0.01$ | 0.06 | $0.16 \pm 0.11$ |
| V | 0.65 | $0.04 \pm 0.02$ | 0.06 | $0.09 \pm 0.03$ |
| R | 0.69 | $0.02 \pm-0.02$ | 0.01 | $0.11 \pm 0.04$ |
| I | 0.70 | $0.04 \pm-0.04$ | 0.03 | $0.15 \pm 0.03$ |



Figure 6a. V428 Cep-NGC 188. B (middle), V (bottom) delta magnitude and color magnitudes vs. phase plots in the sense of V-C (top).


Figure 6b. V428 Cep-NGC 188. R (middle), I (bottom) delta magnitude and color magnitudes vs. phase plots in the sense of V-C (top).

Table 5. V428 Cep-NGC 188 light curve solution.

| Parameters | Values |
| :---: | :---: |
| $\lambda_{\mathrm{B}}, \lambda_{\mathrm{V}}, \lambda_{\mathrm{R}}, \lambda_{\mathrm{I}}(\mathrm{nm})$ | 440, 550, 640, 790 |
| $\mathrm{x}_{\text {boll, } 2}, \mathrm{y}_{\text {boll, } 2}$ | $0.643,0.643,0.160,0.160$ |
| $\mathrm{x}_{11,21}, \mathrm{y}_{11,21}$ | $0.647,0.647,0.183,0.183$ |
| $\mathrm{x}_{1 \mathrm{R}, 2 \mathrm{R}}, \mathrm{y}_{1 \mathrm{R}, 2 \mathrm{R}}$ | $0.735,0.735,0.1650 .165$ |
| $\mathrm{x}_{1 \mathrm{l}, 2 \mathrm{~V}}, \mathrm{y}_{1 \mathrm{l}, 2 \mathrm{~V}}$ | $0.797,0.797,0.108,0.108$ |
| $\mathrm{X}_{1 \mathrm{~B}, 2 \mathrm{~B}}, \mathrm{y}_{1 \mathrm{~B}, 2 \mathrm{C}}$ | 0. 852, 0.852, -0.018, -0.018 |
| $\mathrm{g}_{1}, \mathrm{~g}_{2}$ | 0.32 |
| $\mathrm{A}_{1}, \mathrm{~A}_{2}$ | 0.5 |
| Inclination ( ${ }^{\circ}$ ) | $80.9 \pm 0.1$ |
| $\mathrm{T}_{1}, \mathrm{~T}_{2}(\mathrm{~K})$ | $5000,4822 \pm 6$ |
| $\Omega_{1}=\Omega_{2}$ | 2. $634 \pm 0.003$ |
| $\mathrm{q}\left(\mathrm{m}_{2} / \mathrm{m}_{1}\right)$ | $0.4228 \pm 0.0009$ |
| Fill-outs: $\mathrm{F}_{1}=\mathrm{F}_{2}$ | $34.5 \pm 1.5$ \% |
| $\mathrm{L}_{1} /\left(\mathrm{L}_{1}+\mathrm{L}_{2}\right)_{\mathrm{I}}$ | $0.710 \pm 0.002$ |
| $\mathrm{L}_{1} /\left(\mathrm{L}_{1}+\mathrm{L}_{2}\right)_{\mathrm{R}}$ | $0715 \pm 0.002$ |
| $\mathrm{L}_{1} /\left(\mathrm{L}_{1}+\mathrm{L}_{2}\right)_{\mathrm{V}}$ | $0.724 \pm 0.003$ |
| $\mathrm{L}_{1} /\left(\mathrm{L}_{1}+\mathrm{L}_{2}\right)_{\mathrm{B}}$ | $0.734 \pm 0.005$ |
| $\mathrm{JD}_{0}$ (days) | $2456599.6001 \pm 0.0002$ |
| Period (days) | 0. $30790 \pm 0.00007$ |
| $\mathrm{r}_{1}, \mathrm{r}_{2}$ (pole) | $0.445 \pm 0.007,0.30 \pm 0.01$ |
| $\mathrm{r}_{1}, \mathrm{r}_{2}$ (side) | $0.48 \pm 0.01,0.32 \pm 0.01$ |
| $\mathrm{r}_{1}, \mathrm{r}_{2}$ (back) | $0.51 \pm 0.01,0.37 \pm 0.03$ |
| SPOT Parameters |  |
| Spot 1 On STAR 1 | Cool Spot |
| Colatitude ( ${ }^{\circ}$ ) | $75.0 \pm 2$ |
| Longitude ( ${ }^{\circ}$ ) | $39 \pm 1$ |
| Spot radius ( ${ }^{\circ}$ ) | $16.6 \pm 0.5$ |
| Spot T-factor | $0.89 \pm 0.01$ |
| Sum(res) ${ }^{2}$ | 0.125 |



Figure 7. V428 Cep-NGC 188. Chart of solution residuals of mass ratios extending from 0.35 to 3 minimizes near 0.4 .


Figure 8a. V428 Cep-NGC 188. B (middle), V (bottom) synthetic light curve solutions overlaying the normalized flux curves.


Figure 8b. V428 Cep-NGC 188. R (middle), I (bottom) synthetic light curve solutions overlaying the normalized flux curves.


Figure 9a. V428 Cep-NGC 188. Roche Lobe surfaces from our BVRI simultaneous solution, phase 0.00 (the primary eclipse).


Figure 9c. V428 Cep-NGC 188. Roche Lobe surfaces from our BVRI simultaneous solution, phase 0.50 .


Figure 9b. V428 Cep-NGC 188. Roche Lobe surfaces from our BVRI simultaneous solution, phase 0.25 .


Figure 9d. V428 Cep-NGC 188. Roche Lobe surfaces from our BVRI simultaneous solution, phase 0.75 .
a surface temperature of 5000 K for the primary component. The q-search indicates the mass ratio is 0.4 , with a light curve amplitude of $0.76-0.65$ magnitude in B to I, respectively. The secondary component has a temperature of $\sim 4822 \mathrm{~K}$ (K3), which means the secondary is over luminous for its main sequence mass. The fill-out is $35 \%$. The high inclination of $80^{\circ}$ results in a near total eclipse with less than $1 \%$ of the light due to the secondary component at phase 0.5 . It is an A-type

W UMa binary that has not quite reached thermal equilibrium. The primary component was modeled with a moderately sized cool spot region of $16^{\circ}$ radius and a mean T-factor of $\sim 0.89$ ( $\mathrm{T} \sim 4300 \mathrm{~K}$ ) -- not unusual in solar-type binaries.

## 10. Conclusion

Our 2.5-year period study yields little information about the orbital evolution of the binary. However, since the system has strong magnetic activity, over time, the system should slowly coalesce due to magnetic braking as it loses angular momentum due to ion winds moving outward on stiff magnetic field lines rotating with the binary (out to the Alfvén radius). If the mass ratio becomes more extreme and the fill-out increases, than we would predict the binary will coalesce, producing a rather fast rotating, single A-type main sequence field star (Guinan and Bradstreet 1988). Radial velocity curves are needed to obtain absolute (not relative) system parameters.

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